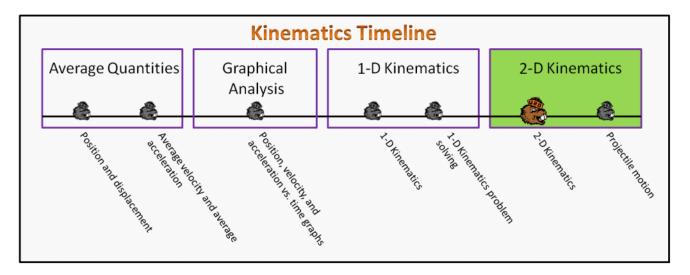
2-D Kinematics Foundation Stage (K1.2)

lecture 1 2-D Kinematics



Textbook Chapters

- BoxSand :: KC videos (2D Kinematics)
- $\circ~$ Giancoli (Physics Principles with Applications 7th) ::~ N/A
- $\circ~$ Knight (College Physics : A strategic approach 3rd) :: N/A
- $\circ~$ Knight (Physics for Scientists and Engineers 4th) ::~ 4.1

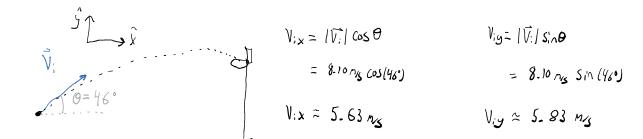
Warm up

K1.2-1:

Description: Find the components of an initial velocity.

Learning Objectives: [?] - Can you identify the objectives from the previous lecture, and this lecture, that this question is relevant to?

Problem Statement: Bernice shoots a 3 pointer releasing the basketball around 8.10 m/s at an angle of 46.0° from the horizontal to the vertical. When the ball is in the air, its acceleration is -g assuming a standard coordinate system. One of the first steps when solving a 2-D kinematics problem is to break vectors into components along the axis you chose for the problem. What are the initial x and y components of the basketball assuming a standard coordinate system?



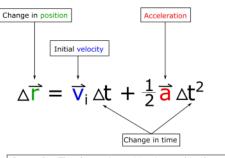
Selected Learning Objectives

- 1. Identify that the motion occurs in more than 1-dimension and requires a 2-D analysis.
- 2. Define a coordinate system that simplifies the complexity of the vector analysis.
- 3. Construct a physical representation the involves multiple dimensions and show a representation of the vector components.
- 4. Demonstrate the ability find the Cartesian components of a vector in the mathematical representation.
- 5. Identify known and unknown quantities for each object, stage, and dimension.
- 6. Solve for a desired unknown in the mathematical representation using a set of kinematic equations for each dimension. Use the problem solving skills developed in 1-D kinematics
- 7. Identify which quantities are the same when comparing two different dimensions, objects, or stages, e.g. elapsed time is the same for both x and y motion.
- 8. Define projectile motion.
- 9. Show that in projectile motion the acceleration has a magnitude of $g = 9.8 \text{ m/s}^2$ and points downward.
- 10. Show that in projectile motion time of flight is determined in an analysis of the vertical motion.
- 11. Show that in projectile motion the horizontal motion can be the same between two cases even when the vertical is not.
- 12. Show that in projectile motion range depends on both the horizontal speed and the time of flight, thus dependent on both the vertical and horizontal analysis.
- 13. Show that in projectile motion the range is the same for complementary angles.
- 14. Show that in projectile motion any system can be analyzed using only the fundamental kinematics equations for constant acceleration, e.g. you do not need specially derived equations like the *range* equation.
- 15. Apply limiting cases sense-making procedures to check their solutions.

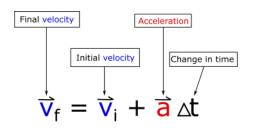
Key Terms

Trajectory

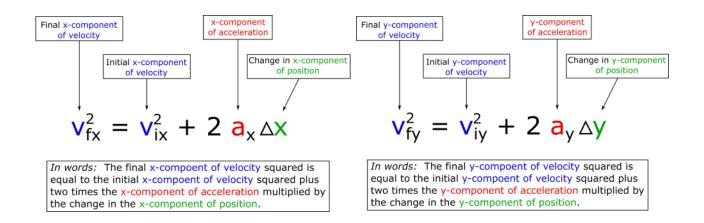
Key Equations



In words: The change in position is equal to the initial velocity multiplied by the change in time plus one-half of the acceleration multiplied by the change in time squared.







Key Concepts

- The kinematics problem solving techniques from 1-D are directly applicable to 2-D problems.
- If an object is moving along a line that is not horizontal or vertical, you can simplify its motion as a 1-D problem rather than a 2-D problem.
- Known and unknown lists help organize kinematic information as well as your thoughts.
- It is highly recommended to not attempt to do algebra (i.e. re-arrange kinematic equations and/or plug them into each other) until you have identified the same number of equations as you have unknowns.
- Recall that time is a scalar; there is no x-component of time or y-component of time, there is only one time which is the same value for both the x and y kinematic analysis.

Act I: 2-D Kinematics

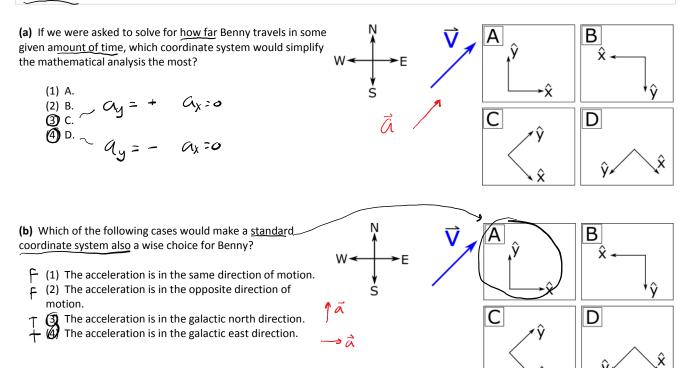
Questions

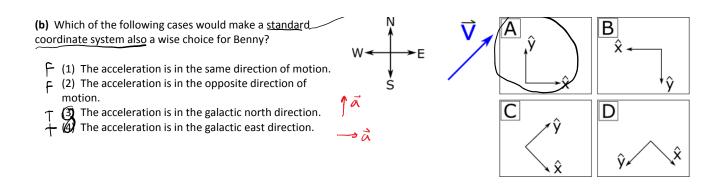
K2.2-2:

Description: Choose a coordinate system that simplifies the mathematical representation. (3 minutes + 3 minutes)

Learning Objectives: [1, 2]

Problem Statement: Benny is in a scooty puff jr spaceship and moving in the galactic northeast direction, when it <u>speeds up in the</u> same direction.





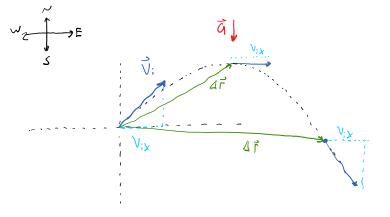
K2.2-3:

Description: Construct a physical representation from a written description. (5 minutes)

Learning Objectives: [1, 3]

Problem Statement: A spaceship is traveling in the galactic northeast direction. The ship's thrusters then create a large constant acceleration in the galactic south direction. Which of the following statements are *necessarily* true regarding the time after the thrusters have fired?

- (1) The ship will be moving in the southeast direction.
- F (2) The ship will eventually be moving in the galactic south direction.
- (3) The ship's displacement will be in the galactic south direction.
- τ (4) The ship will eventually be moving with both southern and eastern components.
- r (5) The change in the ship's velocity will be in the southern direction.



K2.2-4:

Description: 2-D kinematics problem solving for displacement. (6 minutes + 2 minutes + 2 minutes + 5 minutes + 1 min + 4 minutes + 2 minutes + 5 minutes)

Learning Objectives: [1, 3, 4, 5, 6, 7, 15]

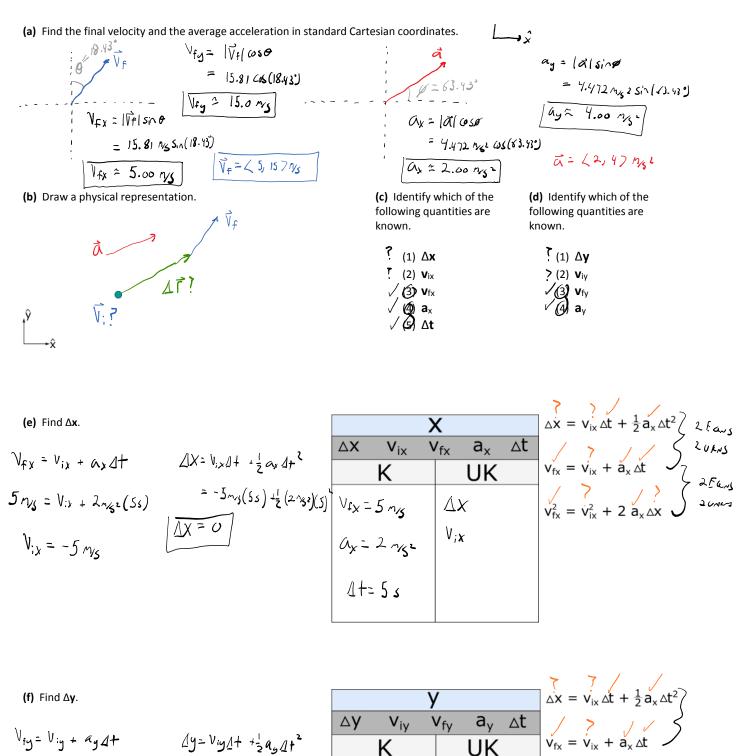
Problem Statement: A spaceship's controls fail for 5.00 s and during this time the thrusters on the ship give it an acceleration of 4.472 m/s^2 in a direction 63.43° from the positive x-direction towards the positive y-direction. They know that after the incident the ship was traveling with a speed of 15.81 m/s in a direction 18.43° from the positive y-direction towards the positive x-direction.

(a) Find the final velocity and the average acceleration in standard Cartesian coordinates.

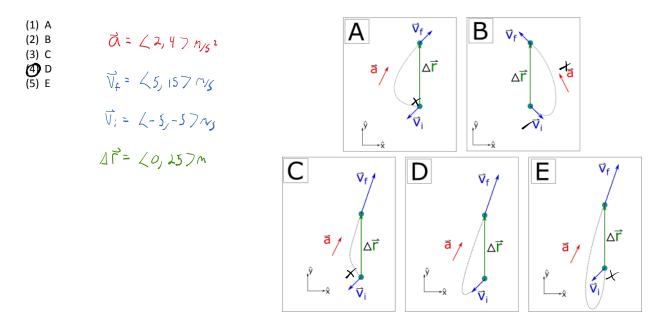
Vfy= |Vf1 (050

đ

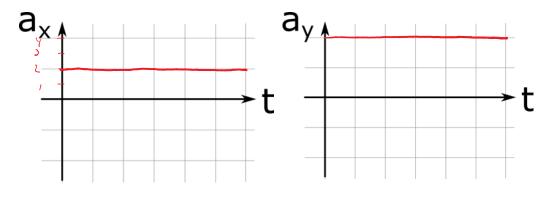
ay = lalsing



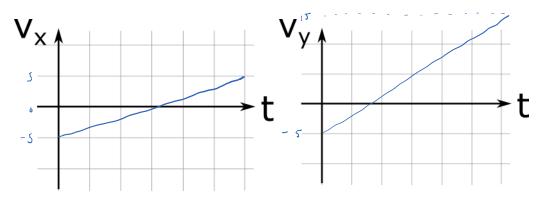
(g) Which of the following figures are a correct physical representation including trajectory (dotted line)?



(h) Sketch the acceleration as a function of time for both the x and y components.



(i) Sketch the velocity as a function of time for both the x and y components.



Conceptual questions for discussion

- 1. Do you agree with the following statement? *If the velocity of an object is not horizontal or vertical then a 2-D kinematic analysis is required.*
- 2. If a spaceship has an initial velocity in the galactic north direction and a thruster that can only provide an acceleration in the galactic east direction, can the spaceship ever travel in the galactic east direction?

Hints

K2.2-1: No hints.

K2.2-2: Can you choose a coordinate system to avoid breaking vectors into components?

K2.2-3: Draw a physical representation. If an object has a velocity in the x-direction and no acceleration in the x-direction, does the velocity in the x-direction ever change?

K2.2-4: No hints.